

Course guide

295904 - FGED - Green Functions and Linear Differential Equations: Diffusive Problems, Static Inverters

Last modified: 27/05/2024

Unit in charge: Barcelona East School of Engineering
Teaching unit: 749 - MAT - Department of Mathematics.

Degree: Academic year: 2024 **ECTS Credits:** 6.0
Languages: Catalan, Spanish

LECTURER

Coordinating lecturer: Encinas Bachiller, Andres Marcos

Others: Segon quadrimestre:
ANGELES CARMONA MEJIAS - M11
ANDRES MARCOS ENCINAS BACHILLER - M11
M. JOSÉ JIMÉNEZ JIMÉNEZ - M11

PRIOR SKILLS

It is advisable to have passed the subject of Càlcul Numèric i Equacions Diferencials

DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES

Specific:

CEB-01. Solve mathematical problems that may arise in engineering. Apply knowledge of linear algebra; geometry; differential geometry; differential and integral calculus; differential equations and partial differential equations; numerical methods; numerical algorithms; statistics and optimisation.

Generical:

CG-03. (ENG) Conocimiento en materias básicas y tecnológicas, que les capacite para el aprendizaje de nuevos métodos y teorías y les dote de versatilidad para adaptarse a nuevas situaciones.

CG-04. (ENG) Capacidad de resolver problemas con iniciativa, toma de decisiones, creatividad, razonamiento crítico y de comunicar y transmitir conocimientos, habilidades y destrezas en el campo de la Ingeniería Industrial.

Transversal:

01 EIN N3. ENTREPRENEURSHIP AND INNOVATION - Level 3. Using knowledge and strategic skills to set up and manage projects. Applying systemic solutions to complex problems. Devising and managing innovation in organizations.

07 AAT N3. SELF-DIRECTED LEARNING - Level 3. Applying the knowledge gained in completing a task according to its relevance and importance. Deciding how to carry out a task, the amount of time to be devoted to it and the most suitable information sources.

TEACHING METHODOLOGY

-2 hour lectures (approximately): the teacher will describe basic concepts and materials, will give examples and will propose exercises.

- 1 hour (approximately) of the weekly class time will be devoted to solving problems proposed both in class and in the course's ancillary material. Students are required to actively participate in these classes.

- 1 hour, students will be carrying out complementary activities at computer classroom

LEARNING OBJECTIVES OF THE SUBJECT

The objective of this course is to present the concept of solving a linear differential equation of one or several variables under concentrated actions, and how to use this type of solutions to obtain the response to distributed actions. Also, we will focus on the problem of obtaining the coefficients of the equations involved from the knowledge of the corresponding Green function. We will study actual problems of interest in all the degrees taught in the EEBE, which include static problems, diffusive and undulatory problems.

STUDY LOAD

Type	Hours	Percentage
Self study	90,0	60.00
Hours small group	15,0	10.00
Hours large group	45,0	30.00

Total learning time: 150 h

CONTENTS

Green function for initial value problems in one dimension

Description:

Obtaining the Green function. Concentrated actions Dirac Delta. Distributed actions. Lagrange formula. Construction of the Green function for first, second and fourth order equations. Recovery of the physical system coefficients from the Green function.

Specific objectives:

Construction of Green's function in compartmental problems. Construction of the response function in RC, RL, RLC circuits and in oscillators.

Full-or-part-time: 25h

Theory classes: 5h

Practical classes: 2h 30m

Laboratory classes: 2h 30m

Self study : 15h

title english

Description:

Boundary value problems of second and fourth order. Obtaining the Green function. Reciprocity principle of Betti - Maxwell. Recovery of the physical system coefficients from the Green function. Eigenvalues of self-adjoint boundary problem and Mercer's Theorem.

Specific objectives:

Construction of Green's function in problems of transverse bending of ropes and beams, and longitudinal bars. Calculation of vibration frequencies and associated harmonics.

Full-or-part-time: 50h

Theory classes: 10h

Practical classes: 5h

Laboratory classes: 5h

Self study : 30h

Vectorial Calculus and Green's formulae

Description:

Divergence theorem and integration by parts. Classification of second order linear EDPs. Maximum principle. Boundary value problems and uniqueness of solutions.

Specific objectives:

To identify the problems related to static, diffusive and wave phenomena. Physical interpretation of different boundary conditions.

Full-or-part-time: 25h

Theory classes: 5h

Practical classes: 2h 30m

Laboratory classes: 2h 30m

Self study : 15h

Green's functions for problems in several variables

Description:

Problems in rectangular domains. Method of separation of variables. Concentrated actions in the domain and the boundary. Green's function and resolvent kernels.

Specific objectives:

Construction of the Green function in heat diffusion problems of bars. Construction of the Green function in problems of transverse vibrations of ropes and beams, and longitudinal bars. Calculation of vibration frequencies and associated harmonics. Calculation of the function of Green in rectangles.

Full-or-part-time: 50h

Theory classes: 10h

Practical classes: 5h

Laboratory classes: 5h

Self study : 30h

GRADING SYSTEM

The Grade is calculated through continuous assessment through the presentation of work, exercises and laboratory practices.

Problems: 25%

Jobs: 50%

Laboratory: 25%

BIBLIOGRAPHY

Basic:

- Duffy, Dean G. Green's functions with applications. Boca Raton [etc.]: Chapman & Hall/CRC, 2001. ISBN 1584881100.
- Haberman, Richard. Ecuaciones en derivadas parciales : con series de Fourier y problemas de contorno. Madrid [etc.]: Prentice Hall, cop. 2003. ISBN 8420535346.
- Marcellan, Francisco; Casasus, Luis; Zarzo, Alejandro. Ecuaciones diferenciales : problemas lineales y aplicaciones. Madrid [etc.]: McGraw-Hill, 1990. ISBN 8476155115.
- Kythe, Prem K. Green's functions and linear differential equations: theory, applications and computation. Chapman & Hall/CRC, 2011. ISBN 9781439840085.
- Peral, Irineo. Primer curso de ecuaciones en derivadas parciales. Argentina [etc.]: Addison-Wesley, cop. 1995. ISBN 0201653575.